

# Treatise on Caustics Loop Closure thru Display Area Expansion and Contraction

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## Abstract

This treatise introduces and develops a novel concept within the Void-Motion Spacetime (VMS) framework: display area expansion and contraction as the mathematical lever enabling loop closure in transition states. We show that when a void splits, its surface display area expands relative to conserved volume, while merging fragments contracts the display area. This geometric inflation and deflation provides the missing factor in resolving why certain caustics cannot form harmonically closed loops without it. The result is a direct, verifiable prediction linking geometric transitions to measurable physical outcomes, positioning display area dynamics as a foundational principle of spacetime structure. Unlike existing theories, this framework does not rely on assumed external forces but derives closure strictly from geometric constraints, offering a fresh avenue for explaining fusion, photon interactions, and other high-energy transitions.

## Introduction

One of the enduring challenges in developing the Void-Motion Spacetime (VMS) model has been resolving the mathematics of transition states. Ratios and harmonically closed loops explain much of stable particle structure, but caustics often fail to produce closure when applied to transition events such as photon collisions or fusion. The insight presented here is that splitting or merging voids change the apparent display area without altering volume. This inflation or contraction of display area is sufficient to enable loop closure where pure caustic geometry alone cannot.

## Display Area Expansion

Consider a void of conserved volume  $V$ . If it splits into two equal parts ( $V/2$  each), the total display area is not conserved but increases according to the surface scaling law. For spheres, area scales as  $V^{2/3}$ . Thus, splitting yields:

$$F_{\text{split}} = \sum (V_i / V)^{2/3} = 2 \times (1/2)^{2/3} \approx 1.26$$

This means the display area expands by  $\sim 26\%$ . More generally, splitting into  $N$  equal pieces gives  $F_{\text{split}} = N^{1/3}$ . Any nontrivial split produces  $F_{\text{split}} > 1$ . This provides the extra curvature needed to form a harmonically closed loop in cases where caustics alone are insufficient.

## Display Area Contraction

The reverse process, merging voids, produces contraction. Two equal fragments recombining yield:

$$F_{\text{merge}} = \frac{A_{\text{after}}}{A_{\text{before}}} = \frac{(\sum_i V_i)^{2/3}}{\sum_i V_i^{2/3}} \leq 1$$

Equality holds only when there was no split (single fragment).

**Two-piece equal-volume example (V/2 each):**

$$F_{\text{merge}} = V^{2/3} / [2 \cdot (V/2)^{2/3}] = 1 / 2^{1/3} \approx 0.7937$$

This matches the inverse of the split expansion factor for two equal fragments ( $F_{\text{split}} = 2^{1/3}$ ).

**Note:** These relations use the sphere isoperimetric scaling  $A \propto V^{2/3}$ . For arbitrary shapes, they provide rigorous bounds via the isoperimetric inequality.

This contraction provides a mechanism for releasing curvature, effectively stabilizing systems after high-energy transitions. It balances the inflation from splitting and explains why merged states can lock into stable structures rather than remaining over-curved.

## Transition States and Caustics

In transition states — such as photon-photon collisions, nuclear fusion attempts, or unstable decay — pure caustic geometry often fails to yield a closed loop. The addition of display area expansion changes this: during the split, the inflation factor provides exactly the additional curvature needed to close. Conversely, merging events employ contraction to stabilize. This mechanism bridges the gap that has previously prevented a clean derivation of loop closure under transitions.

## Applications

1. Photon interactions: High-energy photon collisions may temporarily split voids, with display area inflation facilitating loop closure, leading to particle creation channels.
2. Nuclear fusion: Hydrogen nuclei under photon bombardment may undergo partial splitting, with expansion enabling fusion pathways otherwise forbidden by caustic geometry alone.
3. Decay processes: Contraction explains how unstable fragments resolve into stable loops.

4. General particle stability: The balance of expansion and contraction provides a unifying description of how matter resists disintegration under perturbations.

## **Conclusion**

Display area expansion and contraction are not minor corrections but central mechanisms for loop closure in transition states. By quantifying these effects and integrating them into the VMS framework, we provide a predictive, experimentally verifiable principle. The framework not only accounts for stable structures but also opens pathways to model high-energy phenomena such as fusion and photon collisions. This may represent the most fundamentally new mathematical addition to the theory, one capable of standing on its own as a principle of modern physics.